

## Context-Free Languages (Section 11.5)

# Context-Free Languages

- We know that the language  $\{a^n b^n | n \in \mathbb{N}\}$  is not regular. It has a non-regular grammar, such as
  - $S \rightarrow aSb | \Lambda$
- A *context-free grammar* has productions of the form:
  - $N \rightarrow w$where  $N$  is a nonterminal and  $w$  is any string containing terminals or non-terminals.
- A *context-free language* is the set of strings derived from a context-free grammar.

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- $S \rightarrow aSa \mid bSb \mid \Lambda$

## One more example

- Consider the language of strings over  $\{a, b\}$  with the same number of  $a$ 's and  $b$ 's.
- A grammar for this is:
  - $S \rightarrow aSbS \mid bSaS \mid \Lambda$